Paper title: Towards a detailed soot model for internal combustion engines

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Extended summary:

In this work, we integrate previously developed models for engine combustion and soot formation.

The engine code we consider is the Stochastic Reactor Model (SRM), which uses detailed chemistry and takes into account convective heat transfer and turbulent mixing. The main strength of the SRM is its capability of qualitatively predicting emission trends of CO, CO₂, NOx, and unburnt hydrocarbons at reasonable computational cost of 1-2 hours per engine cycle. This enables convenient multi-cycle, sensitivity, and parameter studies.

As soot model, we use SWEEP, a population balance solver based on a Monte Carlo method. One of the most striking features of SWEEP is its ability to accommodate up to thousands of internal coordinates, or in other words highly detailed particle descriptions covering aggregate structure and chemical composition.

In order to couple the two codes, a detailed chemical kinetic mechanism describing the combustion of Primary Reference Fuels (PRFs, mixtures of n-heptane and iso-octane) is extended to include small Polycyclic Aromatic Hydrocarbons (PAHs) such as pyrene, which function as soot precursor species for particle inception in the soot model. The extended chemical kinetic mechanism contains 208 species, about 50 of which are involved in the soot precursor chemistry, and 1002 reactions. We validate the mechanism against a variety of experimental data sets for fuel-rich laminar flames obtained from literature.

The integrated model provides not only averaged quantities as functions of crank angle like soot mass, volume fraction, aggregate diameter, and the number of primary particles per aggregate for example, but also more detailed information such as aggregate and primary particle size distribution functions, and specifics about aggregate structure including images similar to those produced with Transmission Electron Microscopes (TEMs). In addition to that, the chemical composition of soot aggregates is modelled in quite some detail. Surface chemistry, including growth and
oxidation reactions at functional sites on the surface of particles, i.e. edges of PAHs, are taken into account. Since tracking every reaction of every molecule is computationally prohibitive, a statistical representation of PAHs and their functional sites is employed. This chemical description allows for example to plot distributions of aggregate C/H ratio and PAH ring count versus aggregate collision diameter.

The combined model is applied to simulate an n-heptane fuelled Homogeneous Charge Compression Ignition (HCCI) engine which is operated throttled at an equivalence ratio of 1.93 with an Exhaust Gas Recirculation (EGR) rate of about 20%. In-cylinder pressure and heat release predictions show satisfactory agreement with measurements. Particle-laden gases are extracted from within the cylinder through a snatch sampling valve and are analyzed by means of a Scanning Mobility Particle Sizer (SMPS) and a High-Resolution Transmission Electron Microscope (HR-TEM). We find that our simulated aggregate size distributions as well as their time evolution qualitatively agree with those obtained experimentally. It is also seen both in the experiment and in the simulation that soot emissions in terms of mass stem mostly from recirculated aggregates, whereas in terms of number mostly from newly formed ones. The simulation also shows that the largest aggregates are recirculated in the trapped residual gases for possibly several cycles before being emitted from the engine.

An important open question in soot research is the transition from pure gas-phase chemistry to the particulate phase, i.e. molecules held together in a particle through physical forces. In our model, two possible pathways from the gas-phase to the particulate phase are considered: inception, i.e. dimerization of pyrene molecules, and condensation, i.e. addition of a pyrene molecule taken from the gas-phase to an existing particle. We studied how the ratio between the rates of these two processes affects aggregate morphology. In line with expectation, we find that, if inception dominates, aggregates consist of large numbers of very small primary particles, whereas if condensation dominates, aggregates consist of comparatively small numbers of large primaries. We note that the peak of the aggregate size distribution early in the formation phase, which is found here well below 10 nm, moves towards larger sizes with increasing importance of condensation, while the collision diameter of the largest aggregates remains largely unaffected.

The present study focused on fully premixed engine operation. However, we have also taken first steps to extend this work towards operating modes which utilize direct injection such as partially stratified HCCI as well as conventional Compression Ignition Direct Injection (CIDI) engines. The time evolution of the cylinder charge in the Kamimoto diagram, i.e. in equivalence ratio/temperature phase space, proves particularly useful when analyzing emission formation for stratified operation.
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Engine model: SRM

Stochastic Reactor Model (SRM)

\[
\begin{align*}
\frac{\partial}{\partial t} \mathcal{F}(\psi; t) &= -\sum_{j=1}^{S+1} \frac{\partial}{\partial \psi_j} \left[ G_j(\psi) \mathcal{F}(\psi; t) \right] + \sum_{j=1}^{S+1} \frac{\partial}{\partial \psi_j} \left[ \frac{C_\phi(\psi_j - \langle \psi_j \rangle)}{2T} \mathcal{F}(\psi; t) \right] - \\
&\quad -\frac{\dot{V}}{V} \mathcal{F}(\psi; t) - \frac{1}{h} \left[ U(S_{S+1} + h) \mathcal{F}(\psi_1, \ldots, \psi_S, S_{S+1} + h; t) - U(S_{S+1}) \mathcal{F}(\psi; t) \right]
\end{align*}
\]

- Detailed chemical kinetics
- Turbulent mixing
- Convective heat transfer
- Computationally cheap (1-2 CPU-hrs/cycle)

Chemical mechanism: PRF + small aromatics (extended by H. R. Zhang)
208 species, 1002 reactions
PAHs in gas-phase chemistry

- Hongzhi R. Zhang
- Before: PRF+NOx, 157 species
- After: PRF+NOx+ variety of PAHs and highly unsaturated HCs, 208 species
- Validation against fuel-rich flame experiments

COMPUTATIONAL MODELLING GROUP

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Soot model: site-counting

Describe soot particles by $9+N$ dimensional state space (ARS-SC-PP model):

$$E = (C, H, S_a, N_{ed}, N_{zz}, N_{ac}, N_{bay}, N_{R5}, N_{PAH}, PP_{(1-N)})$$

$PP = \text{primary particle list}$
PAH reaction steps

Armchair ring growth

Free edge growth

5-member ring addition

5-member ring free edge desorption

5-member ring desorption

6-member ring desorption

5-member ring conversion at AC

6- to 5-member ring conversion

Oxidation steps: rates from quantum chemistry

Soot in engines!

- HCCI, n-heptane
- Compression ratio 12
- Equivalence ratio 1.93
- Throttled, 20% EGR

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Averaged soot quantities

Simulation

- Total number of soot aggregates
- Average soot aggregate diameter [nm]

Simulation

- Average primary particle diameter [nm]
- Average number of primary particles per aggregate

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Rates of soot processes

Simulation

Simulation

Simulation

Simulation

Rates of soot processes

Simulation

Simulation

Simulation
Aggregate size distributions (I)

Experiment

Simulation

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Aggregate size distributions (II)

Experiment

Simulation

- dN/dlogDp (1/cm³)
- Electrical Mobility Diameter Dp (nm)
- Particles in residual gas

- dN/dlogD (1/cm³)
- Aggregate collision diameter D [nm]

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Aggregate size distributions (III)

Simulation

Temporal evolution of aggregate size distribution

recirculated aggregates

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Role of EGR

Simulation

11 CAD ATDC

65 CAD ATDC

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Sampled aggregates (I)

49.4 CAD ATDC, 129 primaries, coll. diam. 64 nm
Sampled aggregates (II)

Experiment, sampled at ~16 CAD ATDC
Aggregate composition pdfs (I)

large inception rate

CAD = 11.4

large condensation rate

CAD = 11.4

Simulation

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Aggregate composition pdfs (II)

large inception rate

CAD = 11.4

large condensation rate

CAD = 11.4

Simulation

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Inception vs. condensation

large inception rate

large condensation rate

Simulation

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Future engine soot models (I)

• Partially stratified HCCI
• Partially premixed CIDI
• Conventional CIDI
• (Partially stratified) DISI
Future engine soot models (II)

Soot formation in a partially stratified HCCI engine:

![Graph showing probability density function and soot particle size distribution.](image)
Thank you!

Please visit our website:

http://como.cheng.cam.ac.uk